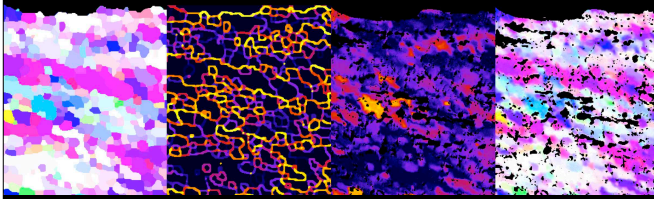


from c-axis to grainsize – my last 50 years of image analysis



renee.heilbronner@unibas.ch

"The Deformation of
Mountains Must Indeed Be Examined With the Microscope"

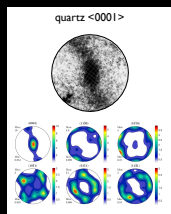
NOTE: change of title !
NOTE: quote Henk Zwart

THANKS go to presidents of TecTask now
IASTG - Enrique Gomez-Rivas, Manish
Mamtani, THANKS go to members of the DRT
organizing committee - Eugenio, Rosalda,
Gaetano

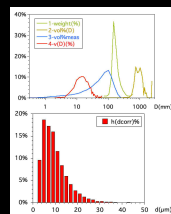
this talk will be about ...

2

c-axis



grain size



... and the use of image analysis

how can we best quantify texture and grain
size ?

this talk will be about how I got close ...
... or not so close ... to answering these
questions
... over the last 50 years

I
decades ago –
before microstructure and
texture analysis went digital

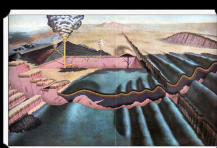
3

Talk
1. pre-computer time
2. to early image analysis (vector graphics,
tablets)
3. to beginning of true digital image analysis
(raster graphics)
4. 3D grainsize
5. CIP meets EBSD
6. about gs
(7. about texture) - this was actually canceled
because of time

when I was young ...

4

A look into my photo album shows my 'direct'
road to geology (...)



my view of geology



my start in geology



stereology and point counting ...

... or how to go from 2D to 3D

find volume density:

Achille Ernest Oscar Joseph Delesse
(1817-1881)

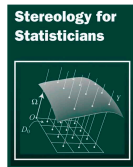
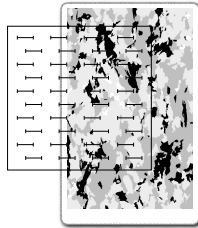
$$V_V = A_A$$

August Karl Rosiwal
(1860-1923)

$$V_V = A_A = L_L$$

Andrei Aleksandrovich Glagolev
(1894-1969)

$$V_V = A_A = L_L = P_P$$



5

All geologists:

F: Delesse: oily paper - tracing - weighing

GB: Sorby: microscope, camera lucida (Amateur naturalist, founder of metallurgy (?)) (1826-1908)

AU: Rosiwal: linear approx. - linear intercept

which is all about probabilities ...



I. Newton



Comte de Buffon
"Mémoire sur le jeu du franc-carreau"



Blaise Pascal



Laplace



A.-L. Cauchy

6

Newton, 1667 (sic!)

Georges-Louis Leclerc Comte de Buffon (1707–1788)

Blaise Pascal, (1623-1662)

Pierre Simon Marquis de Laplace (1745-1827)

Augustin-Louis Cauchy (1789–1857)

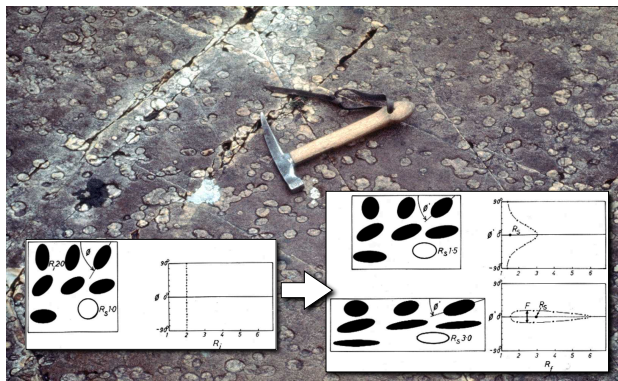
Joseph Emile Barbier (1839-1889)

Sarkis Andreevich Saltykov (1906-)

... stereological theorems

John Ramsay: R_f / φ ...

... or how to measure strain



7

... still no computer involved

John Graham Ramsay CBE FRS (17 June 1931 – 12 January 2021), British structural geologist

Ramsay & Huber, Fig 5.1 R&H showing

Cambrian quartzite with cross sectional areas of deformed worm tubes.

NOTE shape \neq spheres but cylinders !!!

Bruno Sander: AVA*) ...

... or how to map c-axis orientations

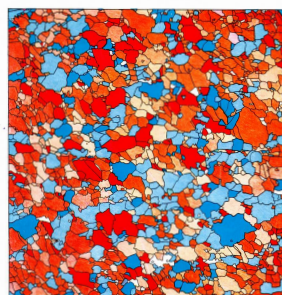
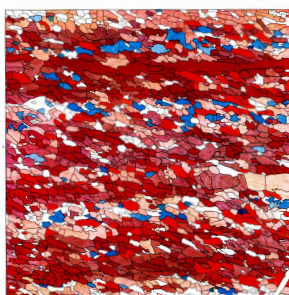


Photo 113. Quartzite, Remington, Idaho: section \perp σ_1 ; 100 \times quartzites: 10, A.V.S. (Remont)

*) Achsenverteilungsanalyse



Photo 113. Quartzite, Remington, Idaho: section \perp σ_1 ; 100 \times quartzites: 10, A.V.S. (Remont)

8

... still no computer involved

Bruno Sander (1884 - 1979) Austrian geologist

Outlines (segmentation) -> mapping (colouring c-axis orientation)

Pole figure is not localized - thermodynamic concept

Procedure:

1. trace boundaries
2. measure CPO on U-stage
3. color stereoplot
4. color grains

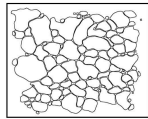
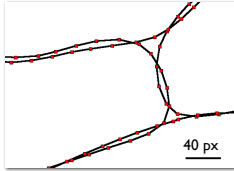
Students and assistants who had to make AVAs called the microscope the "Verblödungsrohre" – they hated it.

2 early 'digital image analysis' (vector graphics)

manual digitisation



boundaries on tablet



polygonal outline (polyline)
defined by:

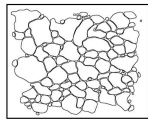
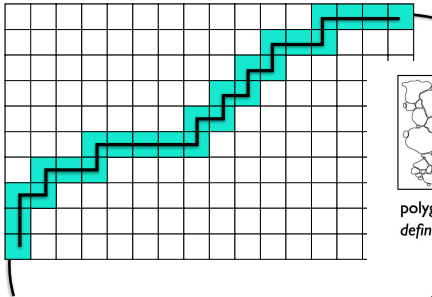
#	x	y
1.	457	11
2.	446	16
3.	432	36
4.	427	49
5.	443	66
6.	484	77
7.	503	68
8.	470	15
9.	457	11
10.	9999	9999
...	etc.	...

vertices of polyline

10

- seventies and early eighties
- 1977 Apple II BASIC
- 1979 Apple tablet
- 1984 Apple Macintosh Pascal
- 1987 NIH Image (Pascal)
- 1993 Image SXM (Pascal)
- 1997 Image J (Java)
- 2007 → Fiji ('Fiji is just ImageJ')

putting the curve on the grid



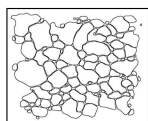
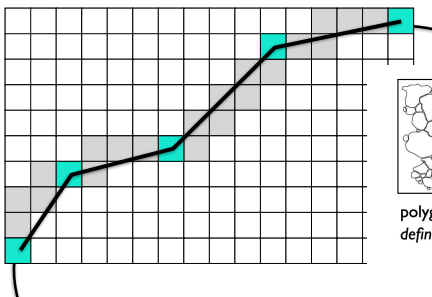
polygonal outline (polyline)
defined by:

#	x	y
1.	457	11
2.	446	16
3.	432	36
4.	427	49
5.	443	66
6.	484	77
7.	503	68
8.	470	15
9.	457	11
10.	9999	9999
...	etc.	...

vertices of polyline

11

try again



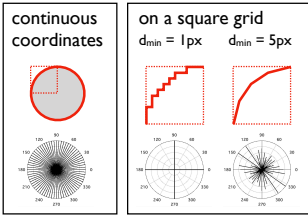
polygonal outline (polyline)
defined by:

#	x	y
1.	457	11
2.	446	16
3.	432	36
4.	427	49
5.	443	66
6.	484	77
7.	503	68
8.	470	15
9.	457	11
10.	9999	9999
...	etc.	...

vertices of polyline

12

"Houston – we have a problem ..."



"Stand by, 13,
... we are looking at it"

```

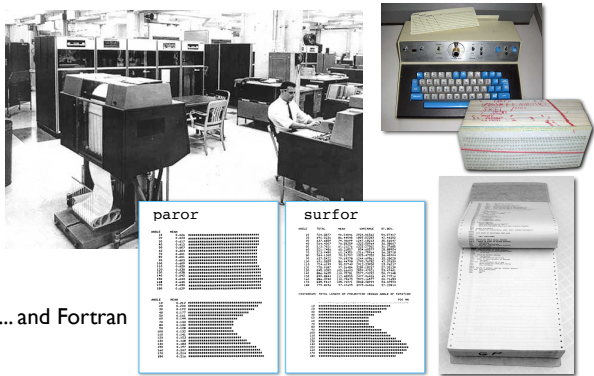
scasmo
-----
*** scasmo [full version]**          2010-10-25, rh
comment: read line file for distance along line
also optional: scaling, smoothing, closing of outlines
also optional: reduction of number of coordinate points
maximum number of points per particle = 4000
particles with less than 7 points are discarded.
input files:
for each particle: x,y
                integer x-y coordinates
                and coordinate (R0-RE)
output files:
line 1:      list
            number of points
for each particle: x,y
                integer x-y coordinates
                and coordinate
    
```

13

Swigert and Lovell reporting the incident on April 13, 1970 — about them same time as scasmo was written (the computer power that drove Apollo 13 easily fits on anybody's mobil phone)

An angle of 1.0° (with tan = 0.1745) requires $\Delta Lx = 57.29$, i.e. 58 pixels
The density of grid points in a given sector of orientations depends on the length of the line and is not constant for all orientations. It is maximal in the horizontal and vertical orientation and changes irregularly with direction, and minimal distance between points.

small data sets – huge computers ...

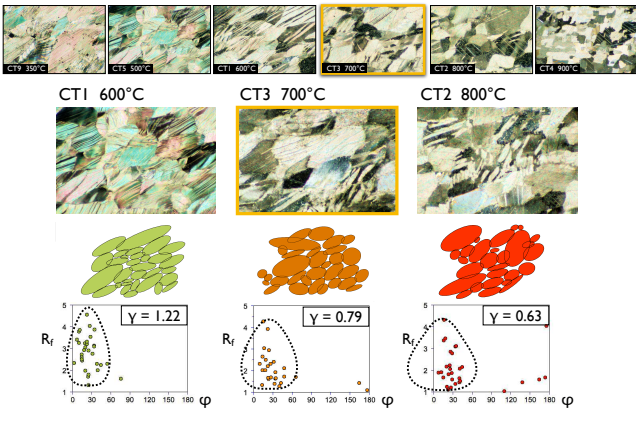


... and Fortran

14

Early 70's - around and after Apollo 13 (1970)

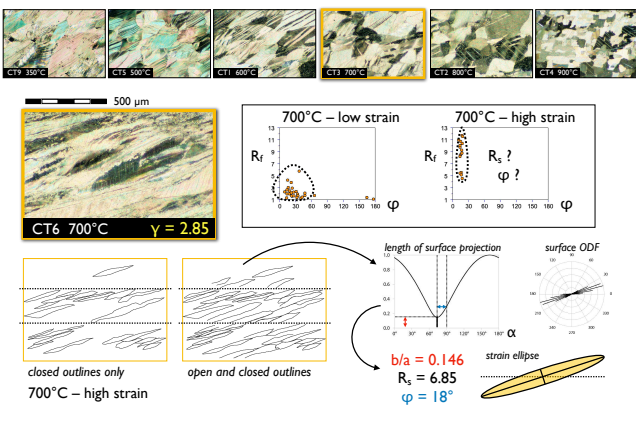
from R_f / ϕ ... when grains were elliptical



15

Schmid, S.M., Panozzo, R. and Bauer, S. (1987)
The strain (R_s) is ver difficult to estimate – especially with the small number of grains available here. Contours are only eye-balled here.

... to SURFOR ... when outlines counted



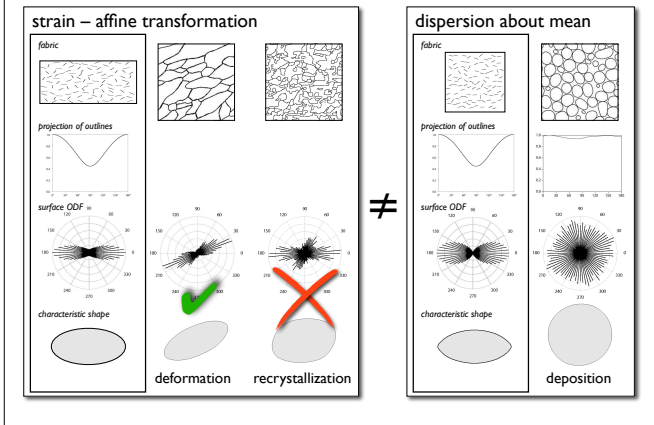
16

Making use of all grain boundary surface – not only of closed outlines.

strain – no strain ? ... "fact or fiction ?"

17

modified after Heilbronner, R. and Barrett, S. (2014). Image Analysis in Earth Sciences - Microstructures and Textures of Earth Materials. Springer Verlag, Heidelberg, 520 p. ISBN: 978-3-642-10342-1 (Print) 978-3-642-10343-8 (Online)



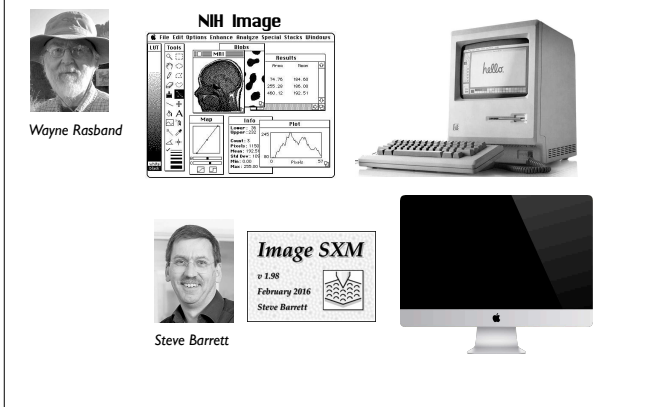
18

3 the beginning of digital image analysis (raster graphics)

19

1987 NIH Image (Pascal)
1997 Image J (Java)
2007 → Fiji ('Fiji is just ImageJ')
1993 Image SXM (Pascal)

time moves on ...



20

With the advent of 'full-scale' digital image analysis, the expectation was that manual outlining could be replaced by automatic segmentation. And that this would open up a number of types of image analysis. 1) looking at connected pixels and boundary pixels, 2) reducing the data to best fit ellipses, 3) deriving polygonal outlines that can be used in the same way as manually digitized outlines.

types of image analysis

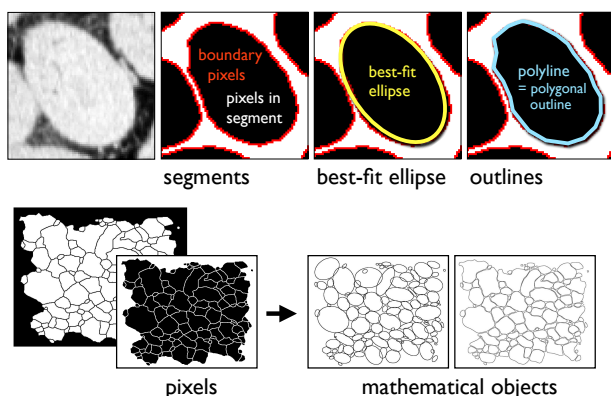
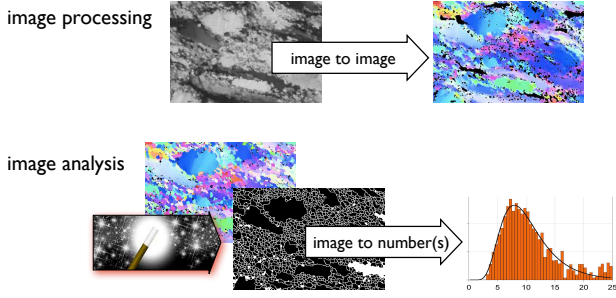


image processing vs. image analysis

21

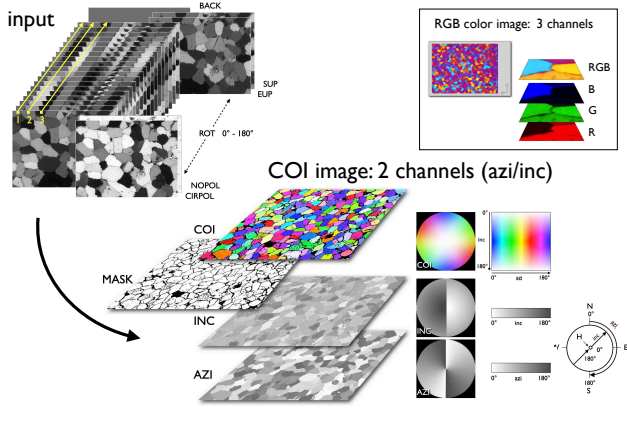
As all participants of my workshops know very well, segmentation is always a big effort. In the context of research where the image material is never the same (as might be in industrial screening, for example) segmentation remains a challenge. There is no such thing as unbiased, automatic segmentation.



some heavy duty image processing

22

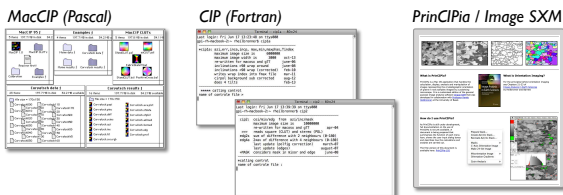
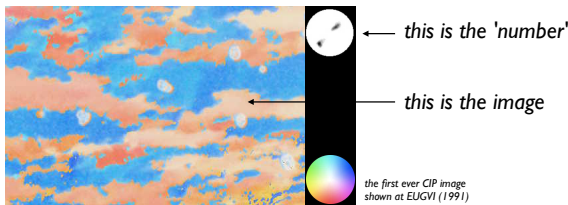
CIP is basically an image processing method which transforms a stack of special input images to an orientation image (image to image). The azimuth and inclination plane provide input for a c-axis pole figure, the first 'analysis' step – in the sense of image to number(s). Orientation images are an excellent basis for segmentation because the threshold can be given in terms of degrees of (mis)orientation. Still, preprocessing is necessary and at almost every step of the process, decisions have to be taken. In addition to visual inspection (for closing outlines, for example) there is a physical basis for the decision (degree of misorientation at the boundary, for example)



from AVA to CIP

23

EUG-VI 1991 – CIP is launched:
CIP = easy AVA procedure = pole figures without U-stage
the first pole figures ... still looked a bit funny



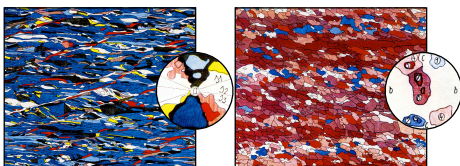
CIP versus AVA

24

we settled for upper hemisphere projection for colouring

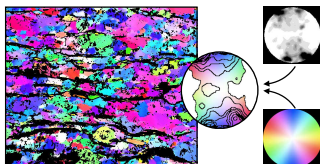
one grain – one c-axis orientation

procedure:
first segment
then color-code



one pixel – one c-axis orientation

procedure:
first color-code
then segment

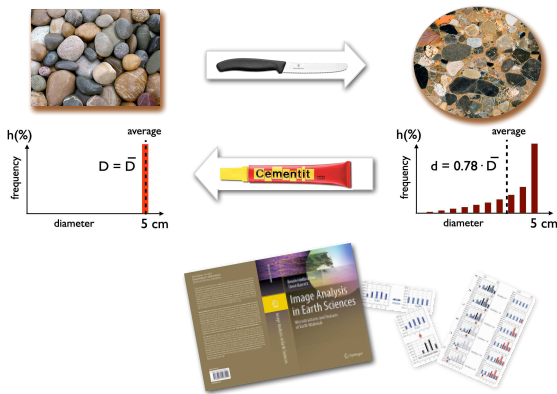


4 3D grain size – an ongoing project

short intro: the tomato salad problem

26

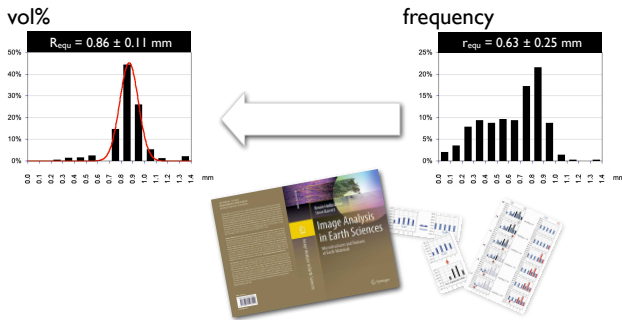
NOTE:
3D grain size distribution has a range of grain size from $d_{min} > 0$ to d_{max}
2D grain size distribution always has d_{min} approaching 0
NOTE:
The 2D distribution can always be calculated, no matter if it is monodisperse, normal, lognormal, bimodal etc.... – the reverse is always impossible.



the effect of using 3D vs. 2D means

27

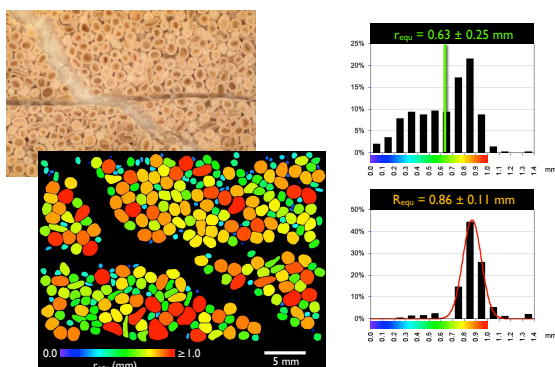
STRIPSTAR
calculates the mode of the volume weighted 3D diameters



... have a look

28

The prevalence – by area – of orange colours indicates that
⇒ 3D mode is closer to the representative grain size
The mean 2D grain size – green colour – is not as prevalent
Blue and green section do not represent small 3D grains, but are sections of larger grains (see absence of small grain in 3D histogram).



5 image analysis today ... by way of an example

looking at deformation experiments ...

Regime #	Y12 % (shear)	Y12 % (anneal)	Mode diam. (μm)	CPO max. (deg)	Mode of strain	Measured porosity	P.A.R.S. (deg)	Grain location (radial, axial)
reg.1	50	100	~7	3.8	BLG			
reg.2	50	100	~8	10.9	SGR			
reg.3	50	100	~14	10.1	GBM			

shearing in dislocation creep regimes 1, 2, and 3 ... and annealing

30

2002 shearing & annealing in regimes 1, 2, 3 – high strain

- regime 1 – BLG – bulging rexl
– low T - high strain rate
- regime 2 – SGR – subgrain rotation rexl
– med T - med strain rate
- regime 3 – GBM – grain boundary migration rexl
– high T - low strain rate

... of Black Hills Quartzite (BHQ)

Regime #	Y12 % (shear)	Y12 % (anneal)	Mode diam. (μm)	CPO max. (deg)	Mode of strain	Measured porosity	P.A.R.S. (deg)	Grain location (radial, axial)
reg.3	50	100	99 ± 12	15 ± 10	reg.3			

shearing in regime 3 only to high strains

31

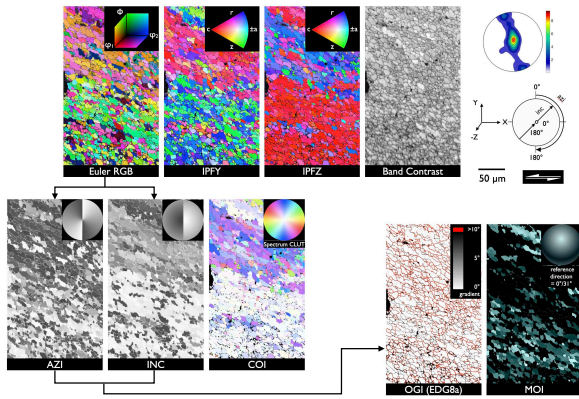
2006 shearing in regime 3 – low to high strain QUESTIONS changing polfig ? changing grain size with gamma ?

in the meantime, CIP meets EBSD ...

32

Bambi Meets Godzilla is a 1969 black-and-white animated short student film created entirely by Marv Newland. Less than two minutes long, the film is a classic of animation; it was listed #38 in the book *The 50 Greatest Cartoons* (1994). See Wikipedia, YouTube.

CIP images from EBSD data

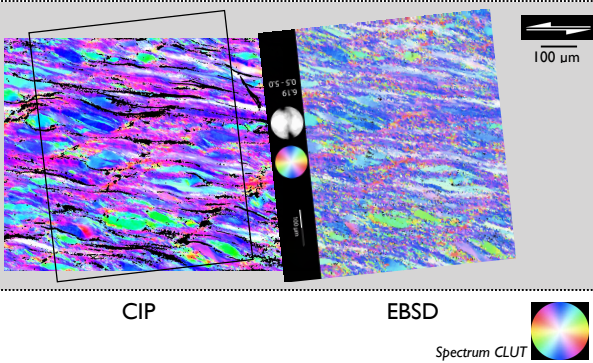


33

COI (showing axis orientation) is more easily interpreted than Euler or IPF coloured maps (showing full crystal orientation)

comparing CIP and EBSD

regime I (w1092) – shearing

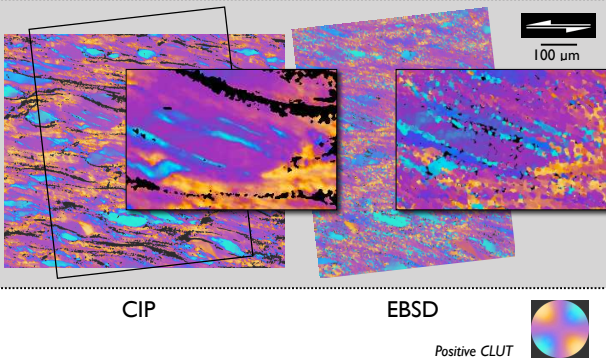


34

EBSD: Obvious improvement of spatial (and orientational) resolution !!
Left: original CIP image, right: EBSD image recalculated for CIP colouring

optical microscopy in the SEM

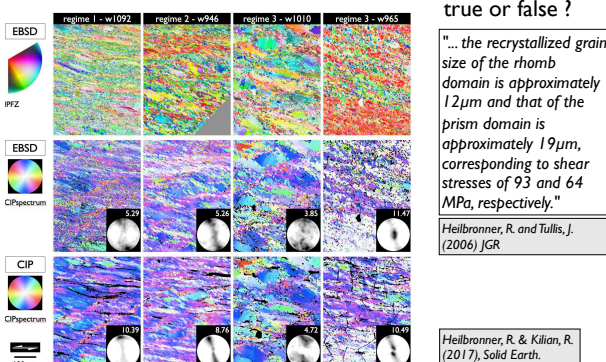
regime I (w1092) – shearing



35

Left: original CIP image using the Positive CLUT, right: EBSD image recalculated for Positive colouring.
=> 'optical polarization microscopy' at EBSD resolution

BHQ revisited



true or false ?

"... the recrystallized grain size of the rhomb domain is approximately 12µm and that of the prism domain is approximately 19µm, corresponding to shear stresses of 93 and 64 MPa, respectively."

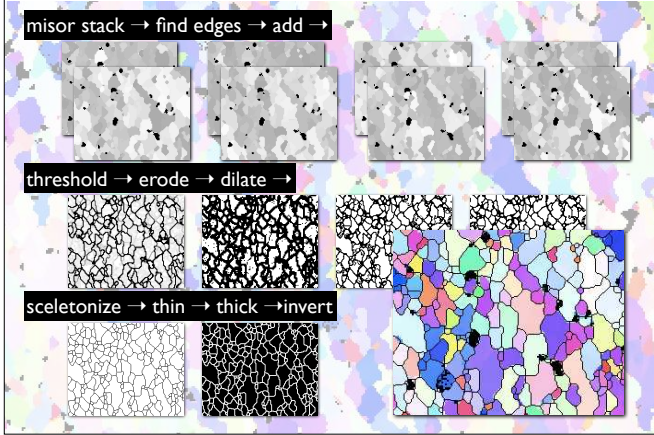
Heilbronner, R. and Tullis, J. (2006) JGR

Heilbronner, R. & Kilian, R. (2017), Solid Earth.

36

NOTE:
For resolution up to 10 µm CIP and EBSD coincide
CIP pole figure = EBSD pole figure ==> note double Y max (≠ an artefact of CIP)
NOTE:
Increasing strain influences polfig:
compare columns at right: both regime 3, left low strain, right high strain (= motivation for 2006 paper)

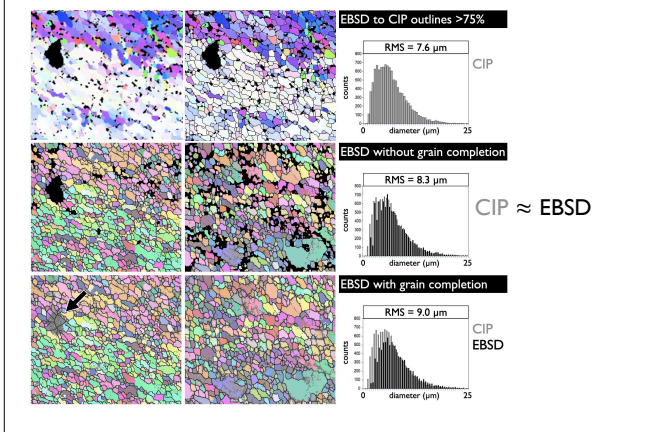
CIP segmentation by shape



37

Procedure to obtain CIP boundaries
Segmentation is carried out using Image SXM and the Lazy Grain Boundaries (LGB) macro (Heilbronner and Barrett, 2014). The input consists of eight c-axis misorientation images (MOI) calculated with respect to four external reference directions and four internal reference directions corresponding to the four most prominent maxima in the pole figure. It looks like magic – but it isn't !

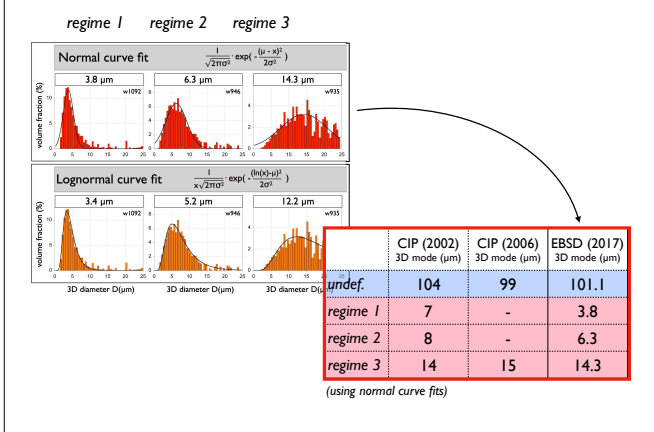
EBSD segmentation by texture



38

RMS instead of mean, following Stipp&Tullis who selected 2D RMS over 2D mean
NOTE:
Segmentation is always difficult and never unbiased !!
grain size distributions as f(procedure)

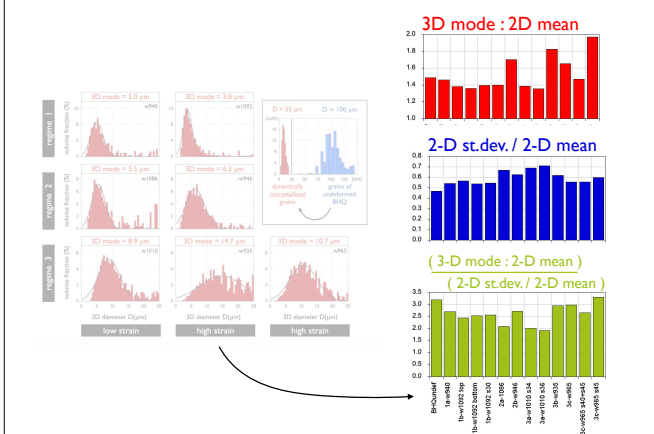
grain size as f(curve fit)



39

Other options: polynomial fit, requires 'eye-balling' to determine mode.

the infamous 'correction factor'

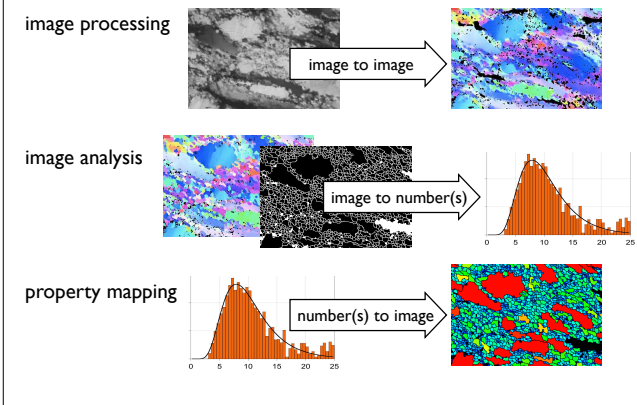


40

IMPORTANT:
do not ever use 'correction factors'

put the numbers back into the picture

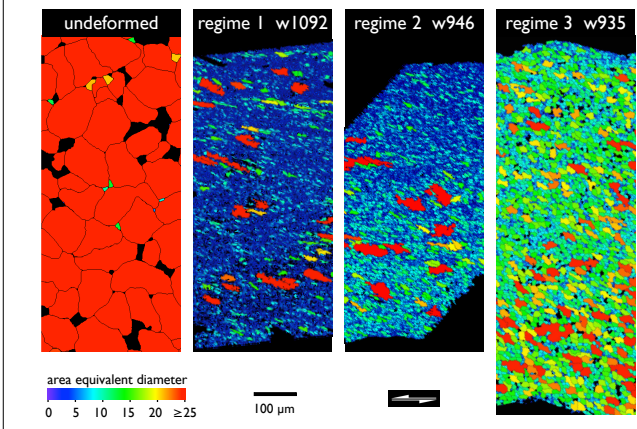
41



grain size mapping

42

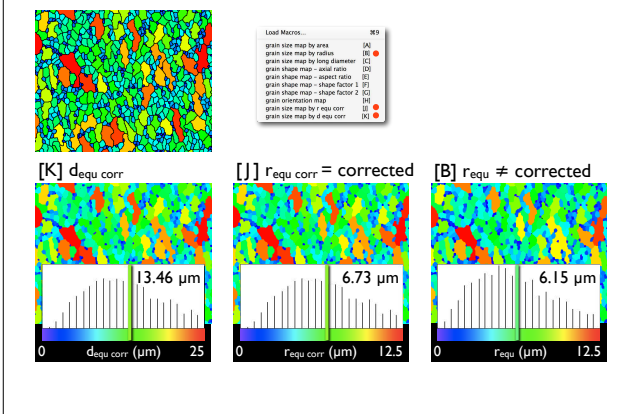
NOTE: grain size gradient in regime 2 experiment



if you are allergic to 3D grain size ...

43

see Heilbronner and Barrett, (2014)

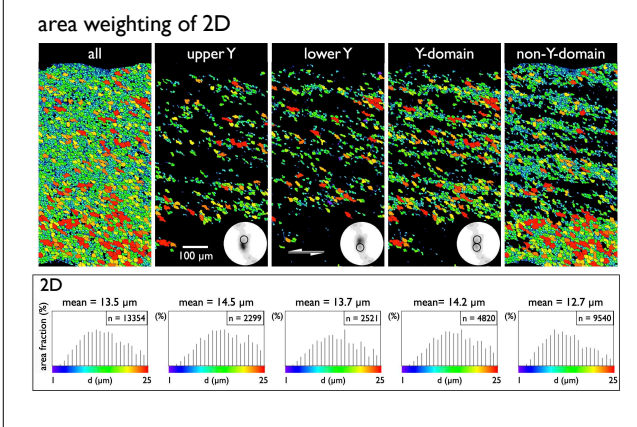


texture dependent grain size

44

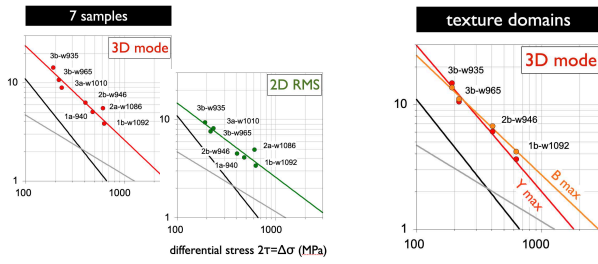
See Heilbronner, R. & Kilian, R. (2017). The grain size(s) of Black Hills Quartzite deformed in the dislocation creep regime. *Solid Earth*, 8, 1071–1093, 2017, doi.org/10.5194/se-8-1071-2017.

NOTE:
area weighting of 2D ≠ volume weighting of 3D



the quartz piezometer(s)

45



piezometer different for shearing vs. axial ?
– unresolved

piezometer different for different domains ?
– unresolved

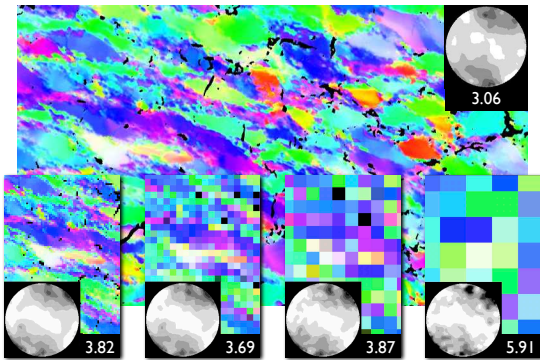


46

texture strength – spatial resolution

47

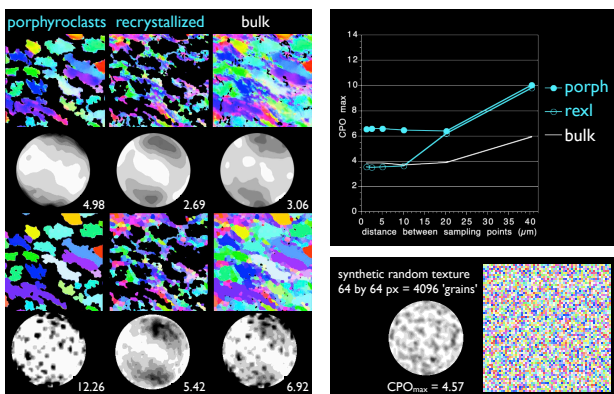
The meaning of pole figure maxima ... if any.



texture strength – grain size

48

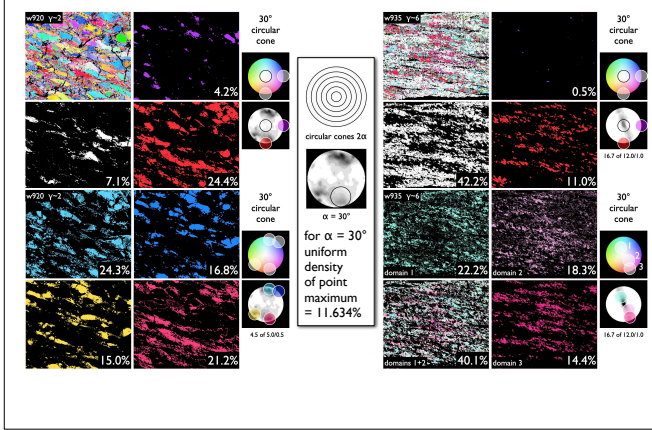
Presented at IAMG 2002
Renée Heilbronner (1), K.Gerald van den Boogaart (2), Helmut Schaeben (2)
Comparison of Coarse- and Fine-Grained Quartz Textures Using the Pole Density Index (PDI)



texture mapping

49

see Heilbronner and Barrett, (2014)



50

so ...?

51

from ellipsoids to surfaces
spatial distribution as important as size
distribution
CIP for mapping - visualization - play =====
EBSD for detail analysis
yes, dont worry just do it right

to summarize

- what has digital added to 'manual' image analysis ?
- what is the relation between Bambi and Godzilla ?
- should we worry about grain size ?
- why should we visualize ?

... in any case

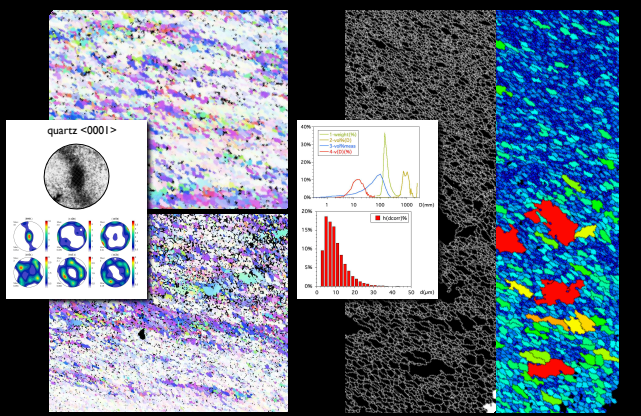
52

Localisation is important! – One (average) number is never sufficient to explain rock behaviour.

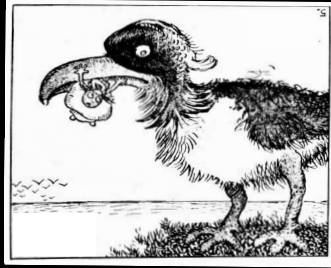
The spatial distribution of grains with a given a size distribution is crucial.

Question, for example: Is the size randomly distributed or layered ? i.e., random, clustered or ordered? isotropic or anisotropic?

... "you can observe a lot by watching"



what image analysis teaches you ...



53

Little Lady Lovekins and Old Man Muffaroo
if you think you know what it is - ... it may be different

Verbeek was of Dutch descent, but born in Nagasaki, Japan in 1867. His father, Guido Verbeck was a missionary for the Reformed Church in America, and later a head of the Tokyo Imperial University. Gustave spent his childhood in Japan, moved to Paris for art school, and eventually to the United States in 1900 for work as an illustrator and cartoonist for Harper's Magazine, The Saturday Evening Post, and The New York Herald. The latter was where The Upside-Downs of Little Lady Lovekins and Old Man Muffaroo premiered on May 25th of 1902.

what image analysis teaches you ...



54

René Magritte: La trahison des images
Image ≠ object shown on it

René François Ghislain Magritte (21 November 1898 – 15 August 1967) was a Belgian surrealist artist.

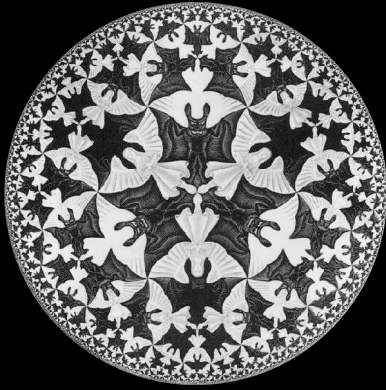
La Trahison des Images is a 1929 painting by Magritte who painted it when he was 30 years old. It is on display at the Los Angeles County Museum of Art.

"The famous pipe. How people reproached me for it! And yet, could you stuff my pipe? No, it's just a representation, is it not? So if I had written on my picture "This is a pipe", I'd have been lying!"
(René Magritte)

what image analysis teaches you ...

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After looking at the black objects, look at what separates them.



... so why use image analysis ?

56

because it makes you ...

... look at your data

... play with your data

you may even solve some problems ...

but most importantly ...

... image analysis makes you ask questions

and finally, ...

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... image analysis has let me meet a lot of nice people,
who have asked a lot of very interesting questions
therefore ...

... thanks go to all participants of all my workshops –
without whom this award would not have been possible

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... thanks go to all participants of all my workshops –
without whom this award would not have been possible